Explain your answers with neat sketches whenever possible. If not clearly stated, assume that the mean radius of the earth is $R=6371 \mathrm{~km}$ if not mentioned.

## Assignment 3-Coordinate Systems

1. Express your views about the following statements.
a. The reason for numerous coordinate systems in geodesy.
b. Deflection of the vertical can be used to convert from natural to geodetic coordinates.
c. There are essential elements to define a coordinate system.
d. Orthometric height is measured along the ellipsoidal normal at the point.
e. The quantities $\Phi, \Lambda$, and $H$ define the position of the observer with respect to the geoid \& the mean rotational axis of the earth.
f. When rectangular system is called Average Terrestrial Coordinate System.
g. Average Terrestrial Coordinate System and geodetic coordinate systems are the same.
h. Observations which define the components of a horizon coordinate system.
2. Calculate the coordinates of a station $C$ in a local coordinate system $U V W$ if the change in rectangular coordinates from $C$ to $D$ is $\Delta X=15 \mathrm{~km}, \Delta Y=10 \mathrm{~km}$, and $\Delta Z=3 \mathrm{~km}$ Also, compute the astronomic azimuth $A_{C D}$, spatial distance $S_{C D}$, and zenith angle $Z_{C D}$ if the deflection components at $C$ are $\xi=5^{\prime \prime}$, and $\eta=3^{\prime \prime}$ while the geodetic coordinates of $C$ are $\varphi=$ $26^{\circ} 15^{\prime} 27^{\prime \prime} N$, and $\lambda=30^{\circ} 25^{\prime} 12^{\prime \prime} E$.
3. Given that the deflection components $\xi, \eta, N$ at an arbitrary station $P$ are $15^{\prime \prime}, 10^{\prime \prime}$, and 12.5 m , respectively. Calculate the rectangular coordinates of station P if its astronomic coordinates are $\Phi=25^{\circ} 18^{\prime} 45^{\prime \prime}, \Lambda=26^{\circ} 22^{\prime} 32^{\prime \prime}$ and $H=155.425 \mathrm{~m}$.
4. If the astronomic coordinates at point 1 are $\left(\Phi_{1}=40^{\circ} 40^{\prime} 10^{\prime \prime}, \Lambda_{1}=41^{\circ} 42^{\prime} 20^{\prime \prime}\right.$ and $\left.\mathrm{H}_{1}=160.50 \mathrm{~m}\right)$ and the measurements from point 1 to 2 not corrected for the gravity effect are $\left(\mathrm{S}_{12}=110.45 \mathrm{~m}, \mathrm{~A}_{12}=20^{\circ}\right.$, and $\left.\mathrm{Z}_{12}=45^{\circ}\right)$. The deflection components at point 1 are $\left(\xi_{1}=15 ", \eta_{1}=9 "\right.$ and $\left.N_{1}=15.50 \mathrm{~m}\right)$. How can the geodetic coordinates $\left(\varphi_{1}, \lambda_{1}, \mathrm{~h}_{1}\right)$, Azimuth $\alpha_{12}$ and Zenith distance $\mathrm{z}_{12}$ can be calculated?
5. Given the geodetic coordinate of two point $\left(\varphi_{A}=30^{\circ} 10^{`} 15^{\prime \prime}, \lambda_{A}=33^{\circ} 20^{\circ} 10^{\prime \prime}\right.$, $\left.\mathrm{h}_{A}=110.12 \mathrm{~m}\right)$ and ( $\left.\varphi_{B}=32^{\circ} 20^{\circ} 05^{\prime \prime}, \lambda_{B}=35^{\circ} 10^{`} 15^{\prime \prime}, \mathrm{h}_{B}=120.10 \mathrm{~m}\right)$. The deflection components at point $A$ are $\left(\xi_{A}=5 ", \eta_{A}=15^{\prime \prime}\right)$ calculate the astronomic azimuth AB ?
